# Neutron Diffraction Study of the Hydrogen-Bond System in $\mathbf{C u}_{2} \mathbf{K}\left(\mathbf{H}_{3} \mathbf{O}_{\mathbf{2}}\right)\left(\mathbf{S O}_{4}\right)_{2}$ 

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#### Abstract

Cu}_{2} \mathrm{~K}\left(\mathrm{H}_{3} \mathrm{O}_{2}\right)\left(\mathrm{SO}_{4}\right)_{2}, \quad M_{r}=393 \cdot 34\), monoclinic, $\quad C 2 / m, \quad a=8.955(2), \quad b=6.265(1), \quad c=$ 7.628 (1) $\AA, \beta=117.45(1)^{\circ}, V=379.8 \AA^{3}, Z=2, D_{x}$ $=3.440 \mathrm{Mg} \mathrm{m}^{-3}, \lambda=0.8307$ (5) $\AA, \mu=0.08 \mathrm{~mm}^{-1}$, $F(000)=141.88$ for cell content, $T=298 \mathrm{~K}, R=$ $0.017, w R=0.011$ for 1285 single-crystal neutron reflections. The structure contains $\mathrm{H}_{3} \mathrm{O}_{2}^{-}$groups with symmetry $2 / m, \mathrm{O} \cdots \mathrm{O}=2.486(1) \AA$; the H atom at the center is split by 0.30 (1) $\AA$. The two O atoms are each bonded to two Cu atoms and are further donors of a weak hydrogen bond of 2.878 (1) $\AA$ to an O atom of the sulfate group.


Introduction. The title compound was investigated previously with X-ray methods by Tardy \& Brégeault (1974) and by Giester \& Zemann (1987). They showed that it is isotypic with the Na member natrochalcite (Rumanova \& Volodina, 1958) and with the exception of the H aioms - located the atoms accurately; Giester \& Zemann (1987) in addition determined approximate coordinates for some of the H atoms. The natrochalcite-type compounds are remarkable in that they can be considered to contain $\mathrm{H}_{3} \mathrm{O}_{2}^{-}$groups (Zemann, 1986; Giester \& Zemann, 1987, 1988; Giester, 1989). Such groups are well known from coordination compounds containing organic radicals (cf. Ardon \& Bino, 1987) and were proposed by Ardon \& Bino (1987) to occur also in a crystal species with formula previously written as $\left[\left(\mathrm{H}_{2} \mathrm{O}\right)\left(\mathrm{NH}_{3}\right)_{3} \mathrm{Cr}(\mathrm{OH})_{2} \mathrm{Cr}\left(\mathrm{NH}_{3}\right)_{3}(\mathrm{OH})\right] \mathrm{Br}_{3} .2 \mathrm{H}_{2} \mathrm{O}$ (Andersen, Nielsen \& Petersen, 1984) on the basis of an $\mathrm{O} \cdots \mathrm{O}$ distance of only $2.45 \AA$ in an $\mathrm{OH}-\mathrm{H}_{2} \mathrm{O}$ configuration. An isoelectronic $\mathrm{H}_{3} \mathrm{~F}_{2}^{+}$group with $\mathrm{F} \cdots \mathrm{F}=2.30$ (1) $\AA$ was recently reported to occur in $\left(\mathrm{H}_{3} \mathrm{~F}_{2}\right)\left(\mathrm{As}_{2} \mathrm{~F}_{11}\right)$ by Mootz \& Bartmann (1988). Only X-ray work seems to have been performed on such compounds until now. Therefore, it seemed interesting to investigate $\mathrm{Cu}_{2} \mathrm{~K}\left(\mathrm{H}_{3} \mathrm{O}_{2}\right)\left(\mathrm{SO}_{4}\right)_{2}$ by neutron diffraction to find the details of the hydrogen-bond system.

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Experimental. Approximately $300 \mathrm{~cm}^{3}$ of an unsaturated aqueous solution with $\mathrm{K}_{2} \mathrm{SO}_{4}: \mathrm{CuSO}_{4} \sim 1: 4$ on a molecular basis were very slowly evaporated in a glass vessel at ca 330 K . Precipitation of green crystals of $\mathrm{Cu}_{2} \mathrm{~K}\left(\mathrm{H}_{3} \mathrm{O}_{2}\right)\left(\mathrm{SO}_{4}\right)_{2}$ began after two weeks, and in two months some of the crystals had grown to the required size.

The crystal used for the neutron measurements had dimensions $\sim 1 \times 3.5 \times 3 \mathrm{~mm}$. Data collection was performed on the four-circle diffractometer P110 at the Orphée reactor in Saclay, wavelength $\lambda=$ 0.8307 (5) $\AA$. Lattice constants were taken from Giester \& Zemann (1987). Data were collected up to $\sin \theta / \lambda=0.974 \AA^{-1} ; 3 \leq 2 \theta \leq 75^{\circ}, \omega$ scans, and $75 \leq$ $2 \theta \leq 108^{\circ}, \omega / 2 \theta$ scans (35 steps, 2 s per step) of widths according to the instrumental resolution: $9-27 \tan \theta+40 \tan ^{2} \theta$; standard reflections ( $0 \overline{4} 0$ and $\overline{8} 03$ ) stable over 14 d within $1 \cdot 3 \%$ (no decay or crystal movement); data-collection index range $h:-17$ to $17, k:-12$ to $0, l:-14$ to 14 . Integrated intensities were determined from resolution adopted profile measurements of the peaks; background was determined by averaging the first and the last six steps on each side. $R_{\text {int }}=0.0135$. The 3444 measured reflections were averaged to give 1561 unique reflections; 1285 of them had $\left|F_{o}\right| \geq 3 \sigma\left(\left|F_{o}\right|\right)$ and were used in the structure refinement.

The least-squares refinement (on $F$ ) with program RFINE4 (Finger \& Prince, 1975) was started in space group $C 2 / m$ with the structural parameters of Giester \& Zemann (1987) for the non-H atoms and H(2); $\mathrm{H}(1)$ was placed at position $2(b)$. Neutron scattering lengths: $b_{\mathrm{K}}=3 \cdot 7, b_{\mathrm{Cu}}=7 \cdot 6, b_{\mathrm{S}}=2 \cdot 85, b_{\mathrm{O}}=5 \cdot 75, b_{\mathrm{H}}$ $=-3.72 \mathrm{fm}$ (International Tables for $X$-ray Crystallography, 1974). The refinement converged for 1285 reflections to $R=0.017, w R=0.011, w=1 / \sigma^{2}(F)$. The shifts of the non-H atoms as compared with the previous X-ray results were very minor. With the exception of $\mathrm{H}(1)$, the anisotropic displacement parameters did not show conspicuous features. For this H atom, the r.m.s. axes were $0.14,0.14$ and $0 \cdot 22 \AA$, practically those of an elongated rotation
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Table 1. Fractional atomic coordinates ( $\times 10^{5}$, e.s.d.'s in parentheses) and equivalent isotropic thermal parameters $\left(\AA^{2} \times 8 \pi^{2}\right)$

| $B_{\text {eq }}=(1 / 3) \sum_{i} \sum_{j} B_{i j} a_{i}^{*} a_{j}{ }^{*} \mathbf{a}_{l} \cdot \mathbf{a}_{j}$. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $x$ | $y$ | $z$ | $B_{\text {eq }}$ |
| K | 2(d) | 0 | $\frac{1}{2}$ | $\frac{1}{2}$ | 1.13 |
| Cu | $4(f)$ |  | 4 | 0 | 0.63 |
| S | 4(i) | 8005 (7) | 0 | 28776 (8) | 0.52 |
| $\mathrm{O}(1)$ | $4(\mathrm{i}$ | 18600 (4) | 0 | 18542 (5) | 0.85 |
| $\mathrm{O}(2)$ | $4(i)$ | 18462 (4) | 0 | 49968 (5) | $1 \cdot 10$ |
| $\mathrm{O}(3)$ | 8() | -2809 (3) | 19442 (4) | 22737 (3) | 0.84 |
| $\mathrm{O}(\mathrm{H})$ | 4(i) | 15621 (4) | 1 | 7523 (5) | 0.68 |
| H(1) | $4(i) \dagger$ | 1876 (38) | $\frac{1}{2}$ | 1207 (114) | 1.63 |
| H(2) | 4(i) | 20284 (10) | $\frac{1}{2}$ | 21942 (10) | 1.93 |
| $\dagger$ Occupancy: $\frac{1}{2}$. |  |  |  |  |  |

ellipsoid [with the rotation axis inclined to the connection line $\mathrm{O}(\mathrm{H}) \cdots \mathrm{O}(\mathrm{H})$ by $\sim 25^{\circ}$. Therefore, the structure was also refined with $\mathrm{H}(1)$ appropriately split at position $4(i)$ with occupancy one half. The least-squares refinement converged again smoothly, even when $\mathrm{H}(1)$ anisotropic displacement parameters were allowed to vary. Final $R$ and $w R$ were as before, and at the end of the refinement all parameter shifts were $<10^{-3}$ of the e.s.d. Within the e.s.d.'s, all coordinates and anisotropic displacement parameters of the non-H atoms and of $\mathrm{H}(2)$ did not change. The connection line of the split $\mathrm{H}(1)$ atom deviated from the direction of the longest axis of the displacement ellipsoid in the preceeding refinement, i.e. with $\mathrm{H}(1)$ on position $2(b)$, by only $5^{\circ}$ : in view of the relatively large error in the localization of the split $H(1)$ a very good agreement. Positional and equivalent isotropic displacement parameters are listed in Table 1.*

Discussion. Table 2 presents interatomic distances and bond angles not involved in the hydrogen-bond system. These agree very well with the X-ray results of Tardy \& Brégeault (1974) and of Giester \& Zemann (1987). For a projection of the structure see, for example, Fig. 1 of Giester \& Zemann (1987).

Great progress was made, as expected, in finding the parameters of the H atoms. Table 3 and Fig. 1 give the geometry of the hydrogen-bond system for the model with $H(1)$ split. The half-occupied $H(1)$ 's are 0.023 (9) $\AA$ off the line connecting the two $\mathrm{O}(\mathrm{H})$ atoms; their mutual distance is 0.30 (1) $\AA$. The main axes of the displacement ellipsoid are $0 \cdot 11,0.14$ and $0 \cdot 17 \AA$; it seems worth mentioning that the shortest axis is not approximately in the direction $\mathrm{O}(\mathrm{H})-\mathrm{H}(1)$, but rather forms an angle of $\sim 30^{\circ}$ with

[^1]Table 2. Bond distances $(\AA)$ and bond angles $\left({ }^{\circ}\right)$ not involved in the hydrogen-bond system
E.s.d.'s are given in parentheses.

|  | $2.7284(3) 2 \times$ | $\mathrm{O}(1)-\mathrm{K}-\mathrm{O}(2)$ | $51.26(1) 2 \times$ | $128.74(1) 2 \times$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{K}-\mathrm{O}(1)$ | $-\mathrm{O}(3)$ | $68.73(1) 4 \times$ | $111.27(1) 4 \times$ |  |
| $-\mathrm{O}(2)$ | $2.8231(3) 2 \times$ | $\mathrm{O}(2)-\mathrm{K}-\mathrm{O}(3)$ | $75.14(1) 4 \times$ | $104.86(1) 4 \times$ |
| $-\mathrm{O}(3)$ | $2.7515(2) 4 \times$ | $\mathrm{O}(3)-\mathrm{K}-\mathrm{O}(3)$ | $88.18(1) 2 \times$ | $91.82(1) 2 \times$ |
|  |  | $\mathrm{O}(1)-\mathrm{Cu}-\mathrm{O}(3)$ | $90.85(1) 2 \times$ | $89.15(1) 2 \times$ |
| $\mathrm{Cu}-\mathrm{O}(1)$ | $2.3515(2) 2 \times$ | $-\mathrm{O}(\mathrm{H})$ | $95.67(1) 2 \times$ | $84.33(1) 2 \times$ |
| $-\mathrm{O}(3)$ | $1.9750(2) 2 \times$ | O |  |  |
| $-\mathrm{O}(\mathrm{H})$ | $1.9830(2) 2 \times$ | $\mathrm{O}(3)-\mathrm{Cu}-\mathrm{O}(\mathrm{H})$ | $89.74(1) 2 \times$ | $90.26(1) 2 \times$ |
| $\mathrm{S}-\mathrm{O}(1)$ | $1.4807(7) 1 \times$ | $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(2)$ | $110.30(4) 1 \times$ |  |
| $-\mathrm{O}(2)$ | $1.4472(7) 1 \times$ | $-\mathrm{O}(3)$ | $108.66(2) 2 \times$ |  |
| $-\mathrm{O}(3)$ | $1.4908(4) 2 \times$ | $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(3)$ | $109.81(2) 2 \times$ |  |
|  |  | $\mathrm{O}(3)-\mathrm{S}-\mathrm{O}(3)$ | $109.58(5) 1 \times$ |  |

Table 3. Bond distances $(\AA)$ and bond angles $\left({ }^{( }\right)$in the hydrogen-bond system
E.s.d.'s are given in parentheses.

| $D-\mathrm{H} \cdots A$ | $D \cdots A$ | $D-\mathrm{H}$ | $\mathrm{H} \cdots A$ | $L D-\mathrm{H} \cdots A$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{O}(\mathrm{H})-\mathrm{H}(1) \cdots \mathrm{O}(\mathrm{H})$ | $2 \cdot 487(1)$ | $1.096(5)$ | $1.392(5)$ | $178(2)$ |
| $\mathrm{O}(\mathrm{H})-\mathrm{H}(2) \cdots \mathrm{O}(2)$ | $2.878(1)$ | $0.980(1)$ | $1.902(1)$ | $174.2(3)$ |
|  |  |  |  |  |
| $\mathrm{H}(1)-\mathrm{O}(\mathrm{H})-\mathrm{H}(2)$ | $107.7(5) 1 \times$ | $\leq \mathrm{S}-\mathrm{O}(2) \cdots \mathrm{H}(2)$ | $173.0(3)$ |  |
| $\mathrm{H}(1)-\mathrm{O}(\mathrm{H})-\mathrm{Cu}$ | $114.4(2) 2 \times$ |  |  |  |
| $\mathrm{H}(2)-\mathrm{O}(\mathrm{H})-\mathrm{Cu}$ | $107.85(4) 2 \times$ |  |  |  |
| $\mathrm{Cu}-\mathrm{O}(\mathrm{H})-\mathrm{Cu}$ | $104.34(2) 1 \times$ |  |  |  |



Fig. 1. Hydrogen-bonding system in projection parallel to [010].
this direction. For $\mathrm{H}(2)$ the r.m.s. axes of the displacement ellipsoid measure $0.13,0.17$ and $0.17 \AA$, i.e. we are dealing with a flattened rotation ellipsoid; its shortest axis almost coincides with the bond direction $\mathrm{O}(\mathrm{H})-\mathrm{H}(2)$. The geometry of the hydrogen-bond system in $\mathrm{Cu}_{2} \mathrm{~K}\left(\mathrm{H}_{3} \mathrm{O}_{2}\right)\left(\mathrm{SO}_{4}\right)_{2}$ agrees with general expectations from the literature (e.g. Olovsson \& Jönsson, 1976; Emsley, 1980; Emsley, Jones \& Lucas, 1981; Chiari \& Ferraris, 1982;

Ferraris, Fuess \& Joswig, 1986; Ardon \& Bino, 1987).

From X-ray investigations it is well known that among the sulfates and selenates of natrochalcite type, the hydrogen-bond lengths vary considerably: $\mathrm{O}(\mathrm{H}) \cdots \mathrm{O}(\mathrm{H})=2.44$ to $2.61 \AA, \mathrm{O}(\mathrm{H}) \cdots \mathrm{O}(2)=2.70$ to $3 \cdot 11 \AA$ (Giester \& Zemann, 1987, 1988; Giester, 1989). Neutron work on further members would provide information on the influence of the chemistry and stereochemistry of the compounds on the geometry of the hydrogen-bond system: a problem of considerable interest. Such investigations have, however, to await the growth of crystals of suitable size.

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# Structure of the Trivanadate $\mathrm{TlV}_{3} \mathrm{O}_{8}$ 

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#### Abstract

Thallium trivanadate, $M_{r}=485 \cdot 2$, monoclinic, $\quad P 2_{1} / m, \quad a=7.780(2), \quad b=8.423$ (3),$\quad c=$ 4.993 (1) $\AA, \beta=96.48$ (2) ${ }^{\circ}, V=325 \cdot 2 \AA^{3}, Z=2, D_{x}$ $=4.957 \mathrm{~g} \mathrm{~cm}^{-3}, \quad$ Мo $K \alpha, \quad \lambda=0.71069 \AA, \quad \mu=$ $2.90 \mathrm{~cm}^{-1}, F(000)=428, T=293 \mathrm{~K}, R=0.049$ for 2032 unique observed reflections. Full isotypy with the known $\mathrm{CsV}_{3} \mathrm{O}_{8}$ structure is found, but e.s.d. values are about four times better. The structure is built from $\mathrm{V}(2) \mathrm{O}_{5}$ square-pyramidal units; these entities share a common edge in order to give condensed $\mathrm{V}_{2} \mathrm{O}_{8}^{6-}$ polyanions. Their corner sharing leads to infinite chains $\left(\mathrm{V}_{2} \mathrm{O}_{7}^{4-}\right)_{\infty}$ lying along the $b$ axis. The $\mathrm{V}(1)$ atoms occupy an octahedral coordination between these chains; the result is a packing of corrugated sheets $\left(\mathrm{V}_{3} \mathrm{O}_{8}^{-}\right)_{\infty}$ parallel to the (100) plane.


Introduction. The hydrothermal treatment of a mixture of $\mathrm{V}_{2} \mathrm{O}_{5}+\mathrm{V}_{2} \mathrm{O}_{3}+\mathrm{Tl}_{2} \mathrm{CO}_{3}+\mathrm{H}_{2} \mathrm{O}$ (mole ratio $0 \cdot 5 / 0 \cdot 12 / 0 \cdot 38 / 99$ ) at 473 K during 24 h in a sealed glass tube leads to three phases: (a) microcrystalline

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tetragonal phase $\mathrm{Tl}_{2} \mathrm{~V}^{\mathrm{IV}} \mathrm{V}_{2}^{\mathrm{V}} \mathrm{O}_{8}$ (Tudo \& Jolibois, 1971; Théobald \& Théobald, 1984); (b) colorless needles of the metavanadate $\mathrm{TlVO}_{3}$ (Ganne, Piffard \& Tournoux, 1974; Howard \& Evans, 1960); (c) red-orange crystals. The crystallographic characterization of the last crystals allowed us to deduce first the composition $\mathrm{TlV}_{3} \mathrm{O}_{8}$ and second their full isotypy with the homologous $\mathrm{K}, \mathrm{Rb}, \mathrm{Cs}$ and $\mathrm{NH}_{4}$ compounds (Kelmers, 1961; Howard, Evans \& Block, 1966). This analogy was suggested on the grounds of powder data (Tudo \& Jolibois, 1971); these last authors obtained $\mathrm{TlV}_{2} \mathrm{O}_{8}$ as a red-orange powder by reaction at 643 K of a mixture of $\mathrm{Tl}_{2} \mathrm{CO}_{3}$ and $3 \mathrm{~V}_{2} \mathrm{O}_{5}$ under inert atmosphere; we show that their published powder data are in accordance with the calculated intensities obtained from our single-crystal study.

Experimental. [001]-elongated prismatic crystal with $\pm(010), \pm(410)$ lateral faces; $0.15 \times 0.07 \times 0.06 \mathrm{~mm}$. Siemens AED2 four-circle diffractometer (graphite monochromator); 26 reflections used for measuring
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[^1]:    * Lists of structure amplitudes and anisotropic displacement parameters have been deposited with the British Library Document Supply Centre as Supplementary Publication No. SUP 52218 ( 32 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

